

MARSHALL PLAN SCHOLARSHIP REPORT

Revised Implementation and Empirical Study of Maximum Likelihood Expectation Maximization Algorithms with and without Superiorization in Image Reconstruction

submitted by

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