

Data Sets of Very Large Linear Feasibility Problems Solved by Projection Methods

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Abstract

We give a link to a page on the Web on which we deposited a set of eight huge Linear Programming (LP) problems for Intensity-Modulated Proton Therapy (IMPT) treatment planning. These huge LP problems were employed in our recent research and we were asked to make them public.

1 Introduction

In our recent research [1, 2] we employed *projection methods* to solve some huge linear feasibility problems that arise in Intensity-Modulated Proton Therapy (IMPT) treatment planning. These huge Linear Programming (LP) problems present a challenge to every LP solver or solution method and we have made the case in our research for tackling them with some elaborate projection methods.

Since the papers [1, 2] are available on the Web we are not going into any further details about the research itself here. We only wish to mention that, in the language of [1]: “The main advantage of projection methods, which makes them successful in many real-world applications, is computational. They

have the ability to handle some huge-size problems of dimensions beyond which more sophisticated methods cease to be efficient or even applicable due to memory requirements. This is so because the building blocks of a projection algorithm are the projections onto the given individual sets, which are assumed to be easy to perform, and the algorithmic structure is either sequential or simultaneous, or in-between, as in the block-iterative projection methods or in the more recent string-averaging projection methods.”

The purpose of this Technical Report, which we do not intend to publish otherwise, is to announce the availability of our data sets for these problems along with detailed instructions where to get them and how to read them. We were asked to post these data sets publicly and we are pleased to do so.

The data sets are accessible from:

http://dig.cs.gc.cuny.edu/~wei/web/?page_id=221.

Please contact chen.wei@mgh.harvard.edu for any related questions.

2 A Set of 8 Huge LP Problems for IMPT

The following is the information for each LP problem associated with *Task0*, *Task1*, ..., *Task7*. For details about these tasks consult the papers where the research is reported [1, 2]. The data are binary, double precision, in the order of a, c, d, e, f, A as in

$$\min \langle a, x \rangle \text{ subject to } c \leq Ax \leq d \text{ and } e \leq x \leq f. \quad (1)$$

The components of the vectors c, d, e, f can be infinite numbers (DBL_MAX in double precision in C language). The sparse matrix A is in column ordered sparse matrix form as described in the MOSEK documentation, which is standard in storage of huge sparse matrix. For example, it can be used in CPLEX and other LP solvers as well. The four arrays of the matrix A are in the order of: *ptrb, ptre, asub, aval*. For a sample C code of how to read the data see the Appendix below.

	#Rows	#Columns	#NonZeros	Objective	Data
Task0	302,491	13,734	62,256,376	MIN	~750M
Task1	314,546	13,734	74,554,123	MAX	~900M
Task2	302,491	13,734	62,256,376	MIN	~750M
Task3	302,491	13,734	62,256,376	MIN	~750M
Task4	302,491	13,734	62,256,376	MIN	~750M
Task5	302,491	13,734	62,256,376	MIN	~750M
Task6	302,491	13,734	62,256,376	MIN	~750M
Task7	604,982	13,734	124,754,745	MIN	~1.5G

3 Appendix

The sample code to read the data in C language:

```

char DataFileName[50] = "./0.dat";
FILE* file = fopen(DataFileName, "rb");
if(file == NULL){
cout<<endl<<"**** fail to open file "<<DataFileName<<" ****"
<<endl;
return 0; }else{
cout<<endl<<"Reading a, c, d, e, f and ptrb, ptre, asub, aval
of A from the binary file "<<DataFileName<<"...";}
fread(a, sizeof(double), numCol, file);
fread(c, sizeof(double), numRows, file);
fread(d, sizeof(double), numRows, file);
fread(e, sizeof(double), numCol, file);
fread(f, sizeof(double), numCol, file);
fread(ptrb, sizeof(int), numRows, file);
fread(ptre, sizeof(int), numRows, file);
fread(asub, sizeof(int), numNonZeros, file);
fread(aval, sizeof(double), numNonZeros, file);
fclose(file);

```

References

- [1] Y. Censor, W. Chen, P.L. Combettes, R. Davidi and G.T. Herman, On the effectiveness of projection methods for convex feasibility problems with linear inequality constraints, *Computational Optimization and Applications*, accepted for publication (<http://arxiv.org/abs/0912.4367>).

- [2] W. Chen, D. Craft, T.M. Madden, K. Zhang, H.M. Kooy and G.T. Herman, A fast optimization algorithm for multi-criteria intensity modulated proton therapy planning, *Medical Physics* **37** (2010), 4938–4945.