SPECTRAL REPRESENTATION OF LOCAL SYMMETRIC SEMIGROUPS OF OPERATORS

AMI VISELTER

ABSTRACT. A spectral integral representation is established for locally defined symmetric semigroups of operators, with indices which are not restricted to a neighborhood of zero. This extends the well-known results of Fröhlich [Unbounded, symmetric semigroups on a separable Hilbert space are essentially selfadjoint, Adv. in Appl. Math. 1 (1980), 237-256] and Klein and Landau [Construction of a unique selfadjoint generator for a symmetric local semigroup, J. Funct. Anal. 44 (1981), 121-137].

DEPARTMENT OF MATHEMATICS, BAR ILAN UNIVERSITY, 52900 RAMAT-GAN, ISRAEL Current address: Department of Mathematical and Statistical Sciences, University of Alberta, Edmonton, Alberta T6G 2G1, Canada E-mail address: viselter@ualberta.ca

²⁰⁰⁰ Mathematics Subject Classification. Primary 47D03, Secondary 47B25.

Key words and phrases. Local semigroups of operators, selfadjoint operators. This paper is a part of the author's Ph.D. thesis, written under the direction of Prof.

Shmuel Kantorovitz in the Department of Mathematics and Statistics, Bar-Ilan University, Israel.